

# [ Money and Inflation (Part 2) ]



EVROPSKÁ UNIE  
Evropské strukturální a investiční fondy  
Operační program Výzkum, vývoj a vzdělávání

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# Demand for Money and QTM

- In equilibrium, the demand for real money balances  $(M/P)_d = kY$  must equal the supply  $M_s/P$ :

$$\underline{M_s/P = kY}$$

$$M(1/k) = PY$$

- which can be written as:

$$MV = PY, \quad \text{where } V = 1/k.$$

- It shows the link between the demand for money and the velocity of circulation of money.
- When people hold a large fraction of their income in the form of money ( $k$  is high), money changes hands less frequently ( $V$  is small).
- When people want to hold only a little money ( $k$  is small), money changes hands more often ( $V$  is large).

# Inflation and interest rates

- Suppose you deposit \$100 in a bank account that pays  $i=8\%$  interest annually. Assume that the price of beer this year is  $P_1=\$2$ .
- Next year, you withdraw your savings and the accumulated interest:  $\$100 \times (1+i) = \$108$
- Assume that the price of beer next year is  $P_2=\$2.04$
- Are you 8 percent richer than you were when you made the deposit a year earlier?
- In the first year, you could buy:  $\$100/\$2 = 50$  bottles
- In the second year, you can buy:  $\$108/\$2.04 = 53$  bottles.
- $\Rightarrow$   $\frac{53-50}{50} = 0.06 = 6\%$  more

**What is the inflation rate in this economy?**

# Inflation and interest rates

$$1 + 0.06 = \frac{\frac{100 \times (1 + i)}{P_2}}{\frac{100}{P_1}}$$

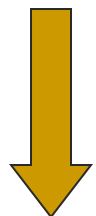
Number of bottles next year = 53

Number of bottles this year = 50

$$1 + 0.06 = \frac{\frac{100 \times (1 + 0.08)}{2.04}}{\frac{100}{2}} = \frac{53}{50}$$

# Inflation and interest rates

$$1 + 0.06 = \frac{\cancel{100} \times (1 + i)}{\frac{P_2}{\cancel{100}} P_1}$$



$$1 + 0.06 = \frac{(1 + i) P_2}{1 P_1}$$



$$1 + 0.06 = \frac{(1 + i) P_2}{P_1}$$

**[ r ... real interest rate ]**

$$1 + r = \frac{(1 + i)}{1 + \pi}$$

$$1 + \pi = \frac{P_2}{P_1}$$

# Inflation and interest rates

- Nominal interest rate,  $i$  ... the interest rate that the bank pays:
  - is not adjusted for inflation
- Real interest rate,  $r$  ... the interest rate that reflects the true increase in the purchasing power (6 % in our example):
  - is adjusted for inflation.

# Inflation and interest rates

$$1 + r = \frac{(1 + i)}{1 + \pi}$$

$$(1 + r) \times (1 + \pi) = (1 + i)$$

$$1 + r + \pi + \pi \times r = 1 + i$$

$$i = r + \pi$$

**Fisher equation**

If we neglect  $\pi \times r = 0.02 \times 0.06 = 0.0012$

$$r = i - \pi$$

# Fisher equation and the Fisher effect

- $i = r + \pi$

*According to the Fisher equation, a 1-percent increase in the rate of inflation in turn causes*

- Hence, in the classical (long-run) theory,
- changes in money growth or inflation do not affect the real interest rate.

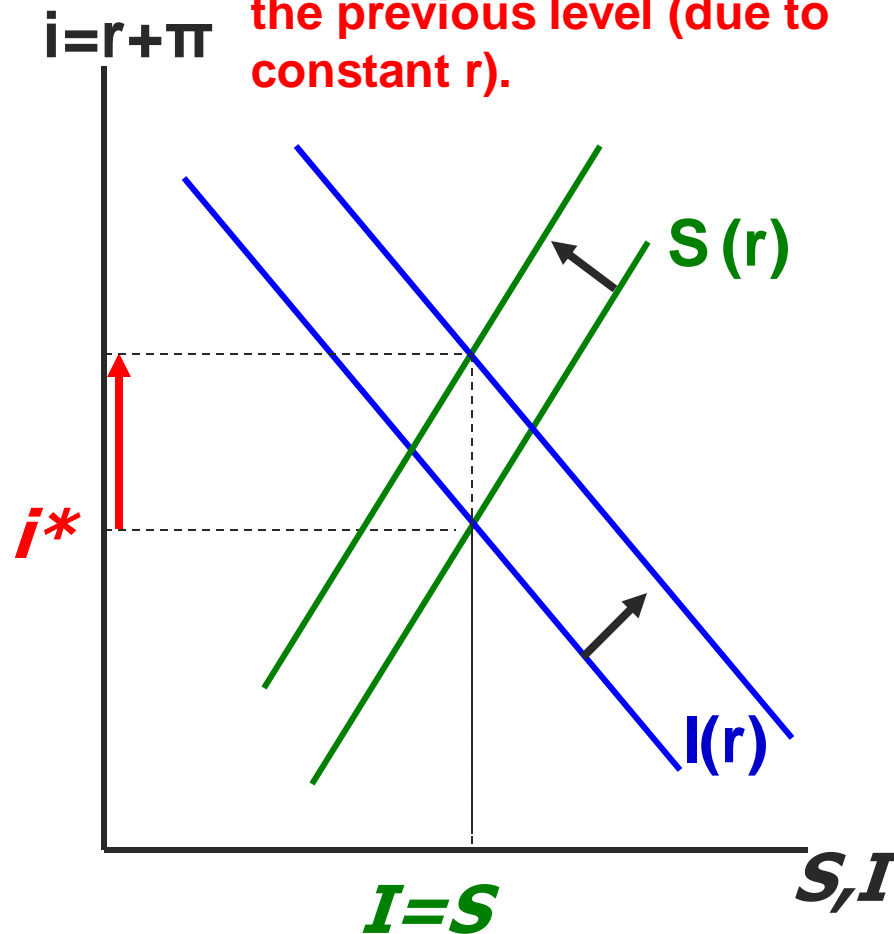
*rate of money growth of 1 percent causes a 1-percent increase in the rate of inflation.*

- The one-for-one relation between the inflation rate and the nominal interest rate is called the **Fisher effect**.



# Fisher effect \*

Nominal interest rate rises keeping the real S and I at the previous level (due to constant r).



Higher inflation rate decreases the willingness of savers to save at the given nominal interest rate  $i$  (their loan will be repaid with money with lower purchasing power).

... Higher inflation increases the willingness of investing firms to (borrow and) invest more at the given nominal interest rate  $i$  (their debts will be repaid with money with lower purchasing power).

# Two Real Interest Rates: *Ex Ante* and *Ex Post*

- When a borrower and lender agree on a nominal interest rate, they do not know what the inflation rate over the term of the loan will be.
- Suppose that they expect  $(\pi^e = 3\%)$ . If the agreed  $r$  is 4%, then:  
 $i = r + \pi^e = 7\%$
- If the realised inflation differs, e.g.  $(\pi = 5\%)$ , then the **ex post real interest rate** will be:
  - $r^{\text{ex post}} = 7\% - 5\% = 2\%$
- Hence, we must distinguish between two concepts of the real interest rate:
  - The real interest rate the borrower and lender expect when the loan is made:
    - ... ***ex ante* real interest rate** =  $i - \pi^e = 4\%$
  - and the real interest rate actually realized:
    - ... ***ex post* real interest rate** =  $i - \pi = 2\%$

Who lost and who gained when  $\pi > \pi^e$ ?

## Two Real Interest Rates: *Ex Ante* and *Ex Post*

- Because the nominal interest rate agreed by lender and borrower can adjust only to expected inflation (not to the realized inflation), the Fisher effect is more precisely written as:

$$i = r + \pi^e$$

- The ex ante real interest rate  $\underline{r}$  is determined by equilibrium in the market for goods and services (or  $I=S$ ).
- The nominal interest rate  $\underline{i}$  moves one-for-one with changes in expected inflation  $\underline{\pi^e}$ .

# Money demand and the nominal interest rate

- In the quantity theory of money, the demand for real money balances depends only on real income  $Y$ .
- Money demand refers to the fraction of wealth the representative agent would like to hold in the form of money.
- Wealth consists of many assets:
  - Bonds, stocks, physical capital (e.g. houses), human capital...

# Money demand and the nominal interest rate

- The other assets typically generate some type of income (e.g. interest income in the case of bonds), but are much less liquid than money.
- The more money the consumer holds in his portfolio, the more interest income he foregoes.
- The less money he holds, the more interest income he makes, but the less liquid is his portfolio.

# Money demand and the nominal interest rate

- The higher the nominal interest rate (e.g. on bonds) the higher is the opportunity cost of holding money.
- Hence,  $\uparrow i \Rightarrow \downarrow$  in money demand.

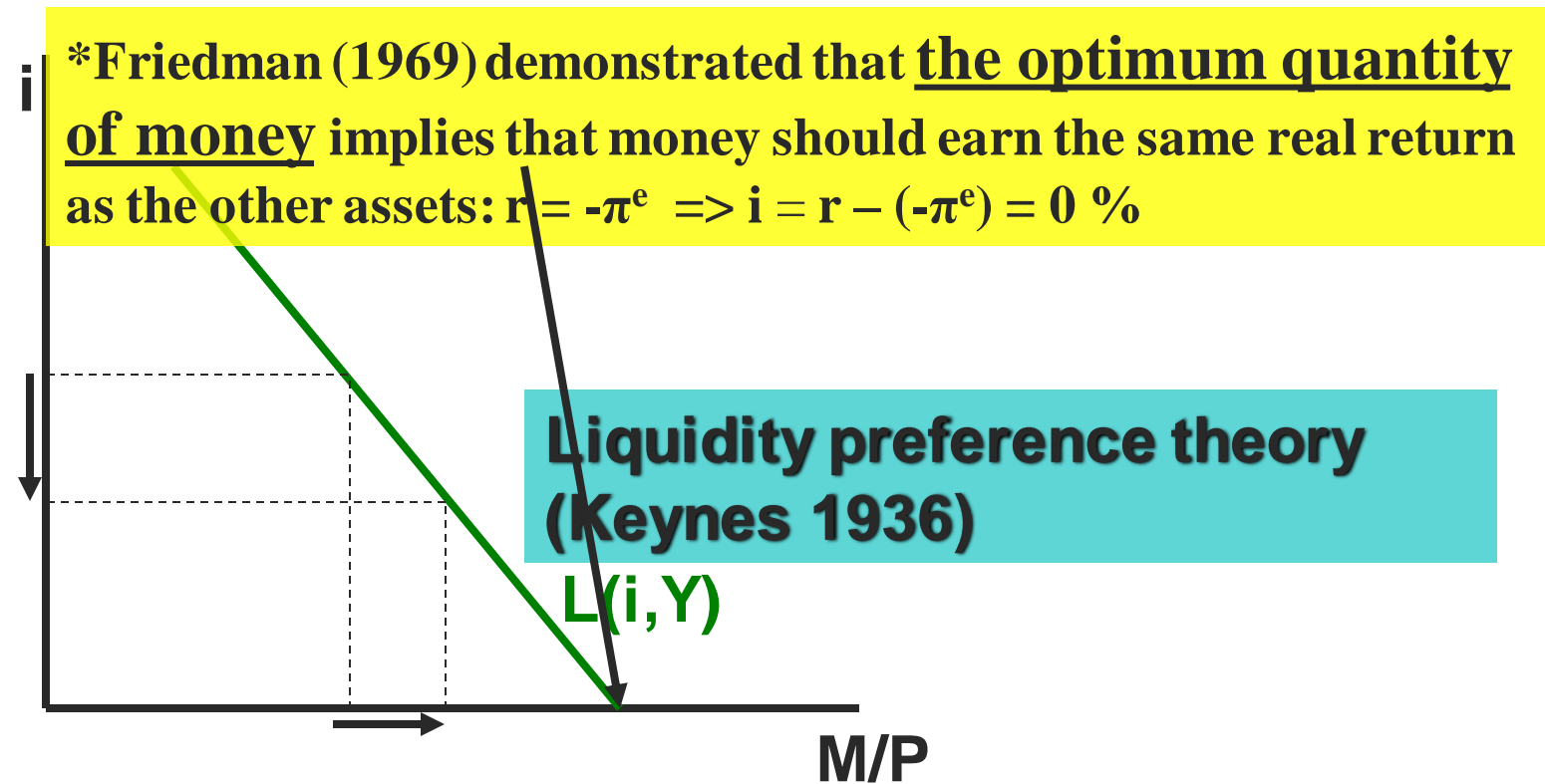
$$(\mathbf{M/P})^d = \mathbf{L}(i, \mathbf{Y})$$

$$L_Y > 0 \quad L_i < 0$$

# Money demand and the nominal interest rate

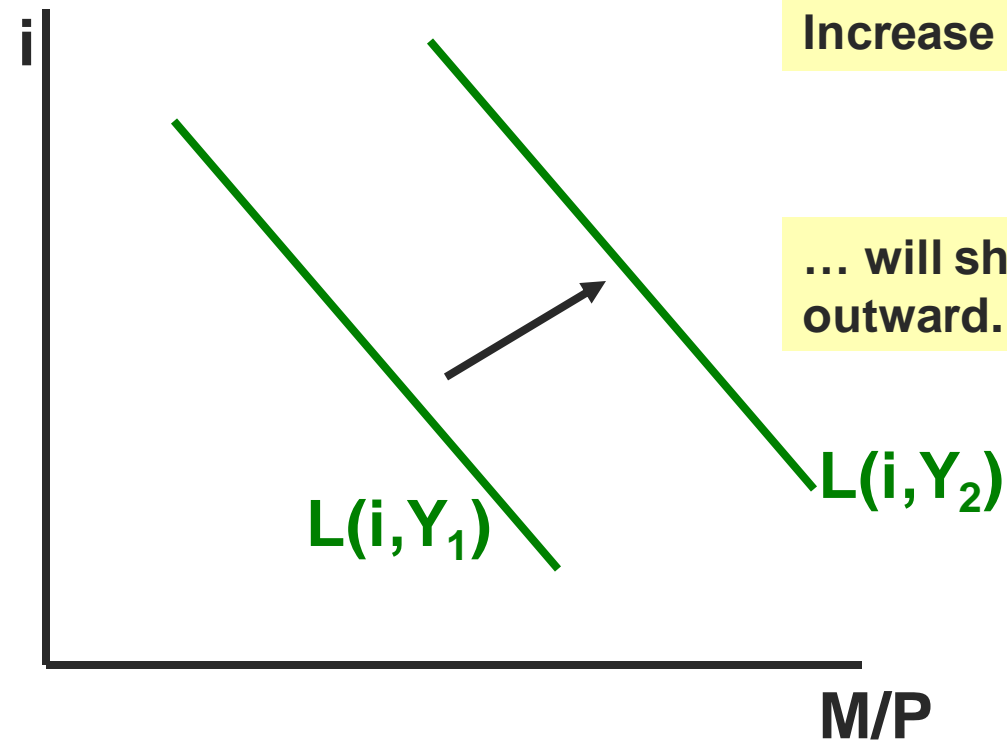
- Why does the **real** demand for money  $L(i, Y)$  depend on the **nominal** interest rate?  
**Notice that during deflation ( $\pi < 0$ ), the real return on money is positive.**
- Money earns an expected real return of  $(-\pi^e)$ , because its real value declines at the rate of inflation.  
**What is the nominal return on money?**
- Assets other than money, earn the real return  $r$ .
- Thus, the cost of holding money is  $r - (-\pi^e)$ , which (as the Fisher equation tells us) is the nominal interest rate  $i$ .

# Money demand and the nominal interest rate

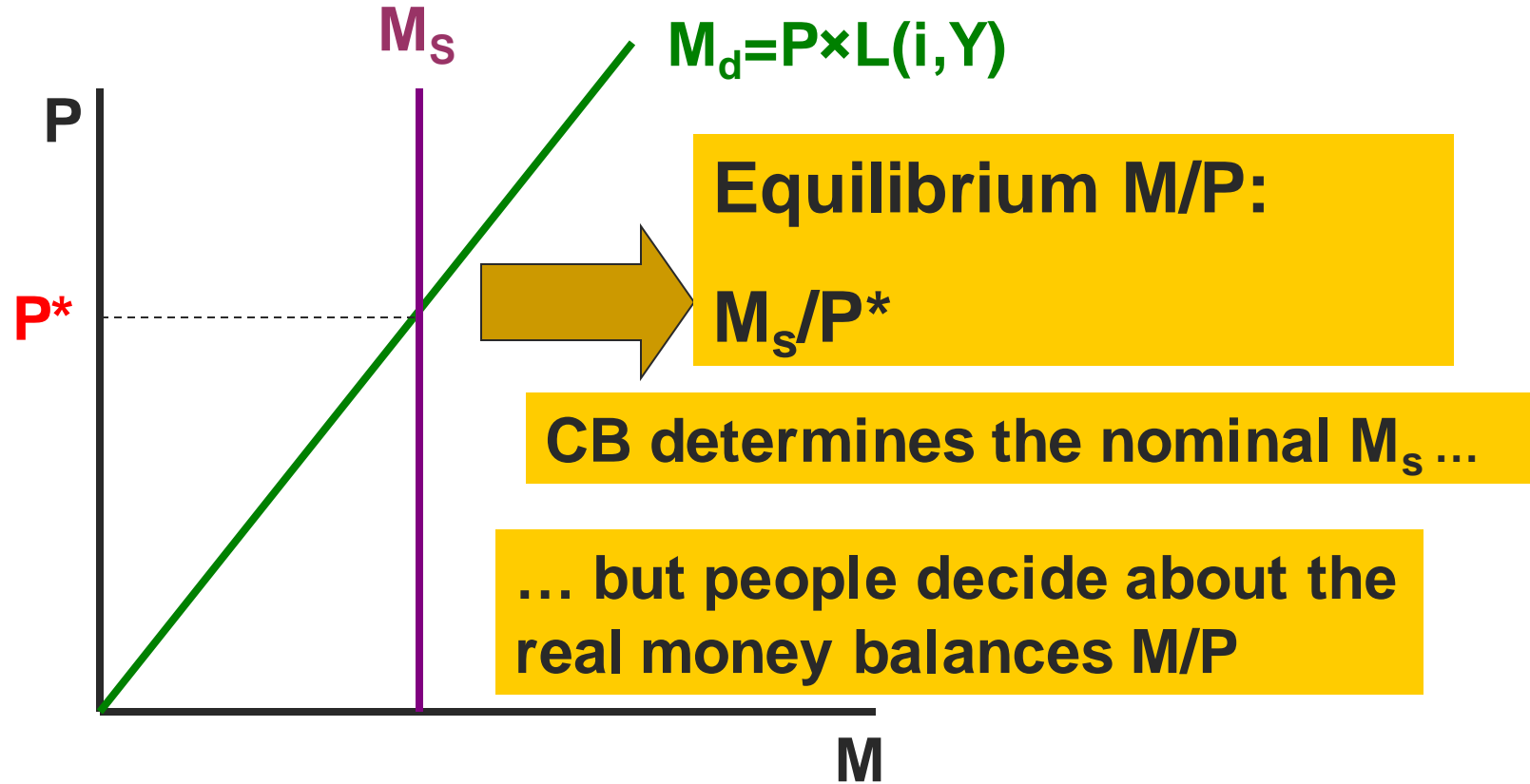




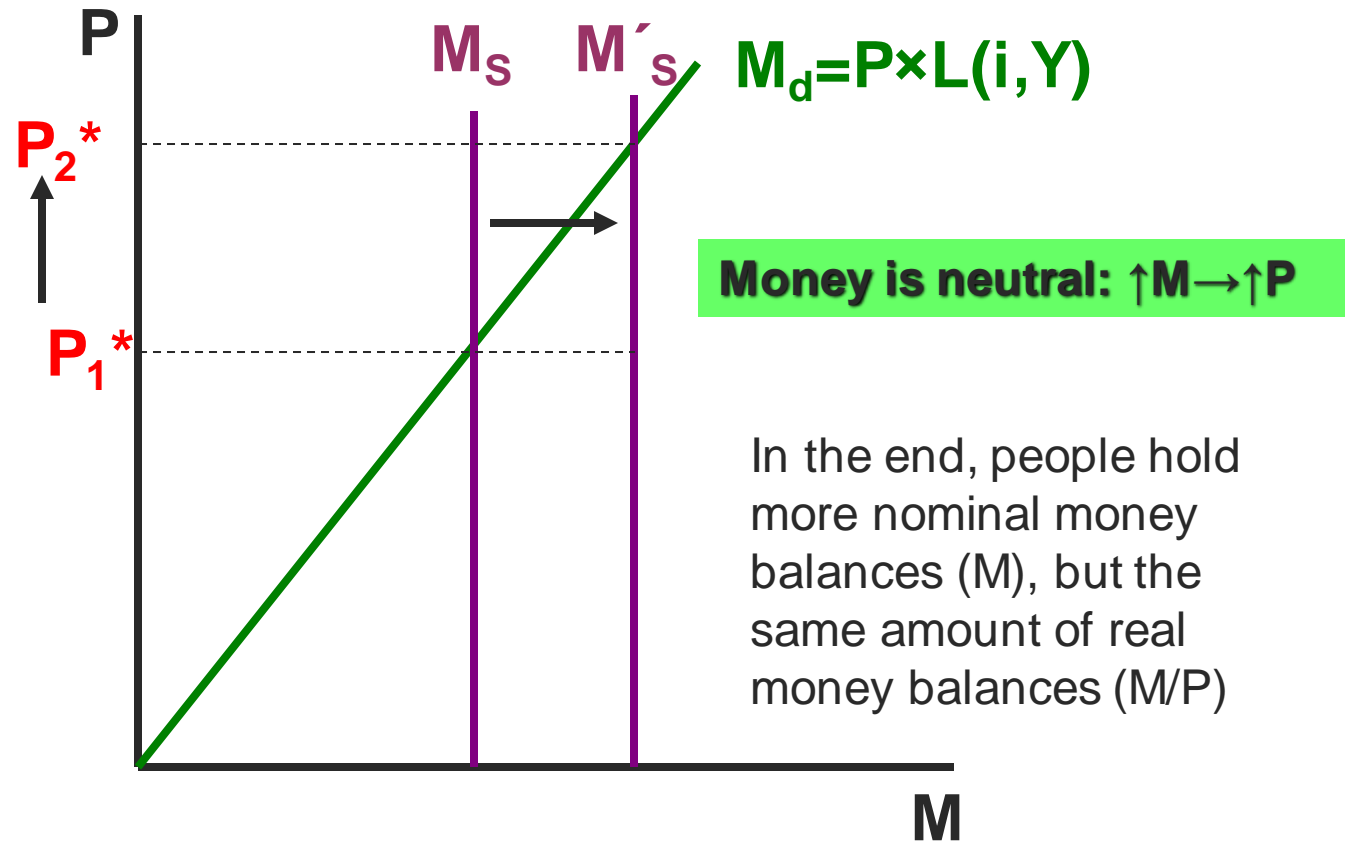
# Money demand and the nominal interest rate



# The equilibrium Price level



# Neutrality of money





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